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# Fundamental Homomorphism Theorems for Neutrosophic Triplet Module

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**Abstract:** In this chapter, our aim is to prove neutro-isomorphism theorems. We define the quotient NT quotient Module and prove the fundamental theorem of neutro-homomorphism. Also, we present and prove the first neutro-isomorphism theorem for neutrosophic triplet Modules, the second neutro-isomorphism theorem for neutrosophic triplet Modules, the third neutro-isomorphism theorem for neutrosophic triplet Modules and a few special cases.

**Keywords:** NT submodule, NT R – module, NT quotient Module, Neutro- homomorphism, neutro-isomorphism

## 1. Introduction

In 1980, Smarandache presented neutrosophy, a part of philosophy. Neutrosophy, which is neutrosophic logic, probability depend on the set in [1]. Neutrosophic logic is the logic of some general concepts such as fuzzy logic presented by Zadeh in [2] and Provided by Atanassov intuitive fuzzy logic in [3]. Fuzzy sets membership function but has an intuitive fuzzy set membership function and non-function and does not define membership indeterminacy. But; neutrosophic set includes all the functions. Many researchers have studied the concept neutrosophic theory and its application to issue multiple-criteria decision analysis in [4-11]. Sahin M., and Kargin A., investigated NT metric space and NT normed space in [12]. Lately, Olgun at al. introduced the neutrosophic module in [13]; Şahin at al. presented Neutrosophic soft lattices in [14]; soft normed rings in [15]; centroid single valued neutrosophic triangular number and its applications in [16]; centroid single valued neutrosophic number and its applications in [17]. Ji at al. searched multi – valued neutrosophic environments and its applications in [18]. Also, Smarandache at al. searched NT theory in [19] and NT groups in [20, 21]. A NT has a form  $\langle m, \text{neut}(m), \text{anti}(m) \rangle$  where;  $\text{neut}(m)$  is neutral of “m” and  $\text{anti}(m)$  is opposite of “m”. Moreover,  $\text{neut}(m)$  is different from the classical unitary element and NT group is different from the classical group as well. Lately, Smarandache at al. investigated the NT field [22] and the NT ring [23]. Şahin at al. presented NT metric space, NT vector space and NT normed space in [24] and NT inner product in [25]. Smarandache at al. searched NT G- Module in [26]. Bal at al. searched NT cosets and quotient groups in [27]. Şahin at al. presented fixed point theorem for NT partial metric space and Neutrosophic triplet v – generalized

metric space in [28-29]. Çelik et al. searched fundamental homomorphism theorems for NETGs in [30] and Çelik et al. Searched neutrosophic triplet R-module in [31]

The concept of an R – module over a ring is a general term of the notion of vector space. The basic structure of Abelian rings, can be more common. Because modular theory is more complicated than the structure of a vector space. Lately, Ai et al. defined the irreducible modules and fusion rules for parafermion vertex operator algebras in [32] and Creutzig et al. introduced Braided tensor categories of admissible modules for affine lie algebras in [33].

In this study, we examine the concept of NT R-Modules. So we obtain a new algebraic structures on NT groups and NT ring. In section 2, we give basic definitions of NT sets, NT groups, NT ring, NT vector space, Neutro-Monomorphism, Neutro-Epimorphism, and Neutro-Isomorphism . In section 3, we define the quotient NT quotient Module and prove the fundamental theorem of neutro-homomorphism. Also, we present and prove the first neutro-isomorphism theorem for neutrosophic triplet Modules, the second neutro-isomorphism theorem for neutrosophic triplet Modules, the third neutro-Isomorphism theorem for neutrosophic triplet Modules and a few special cases. Also, we explain the NT quotient R-module. Finally, in Chapter 4, we give some results.

## 2. Preliminaries

In this section, we present the basic definitions that are important for the development of the paper.

**Definition 2.1:** [21] Let  $N$  be a set together with a binary operation  $\nabla$ . Then,  $N$  is called a NT set if for any  $k \in N$  there exists a neutral of “ $k$ ” called  $neut(k)$  that is different from the classical algebraic unitary element and an opposite of “ $k$ ” called  $anti(k)$  with  $neut(k)$  and  $anti(k)$  belonging to  $N$ , such that

$$k \nabla neut(k) = neut(k) \nabla k = k,$$

and

$$k \nabla anti(k) = anti(k) \nabla k = neut(k).$$

**Definition 2.2:** [21] Let  $(N, \nabla)$  be a NT set. Then,  $N$  is called a NT group if the following conditions hold.

- (1) If  $(N, \nabla)$  is well-defined, i.e., for any  $k, l \in N$ , one has  $k \nabla l \in N$ .
- (2) If  $(N, \nabla)$  is associative, i.e.,  $(k \nabla l) \nabla m = k \nabla (l \nabla m)$  for all  $k, l, m \in N$ .

**Definition 2.3:** [24] Let  $(NTF, \nabla_1, \blacksquare_1)$  be a NT field, and let  $(NTV, \nabla_2, \blacksquare_2)$  be a NT set together with binary operations " $\nabla_2$ " and " $\blacksquare_2$ ". Then  $(NTV, \nabla_2, \blacksquare_2)$  is called a NT vector space if the following conditions hold. For all  $p, r \in NTV$ , and for all  $t \in NTF$ , such that  $p \nabla_2 r \in NTV$  and  $p \blacksquare_2 t \in NTV$  [24];

$$(1) (p \nabla_2 r) \nabla_2 s = p \nabla_2 (r \nabla_2 s); p, r, s \in NTV;$$

$$(2) p \nabla_2 r = r \nabla_2 p; p, r \in NTV;$$

$$(3) (r \nabla_2 p) \blacksquare_2 t = (r \blacksquare_2 t) \nabla_2 (p \blacksquare_2 t); t \in NTF \text{ and } p, r \in NTV;$$

$$(4) (t \nabla_1 c) \blacksquare_2 p = (t \blacksquare_2 p) \nabla_1 (c \blacksquare_2 p); t, c \in NTF \text{ and } p \in NTV;$$

$$(5) (t \blacksquare_1 c) \blacksquare_2 p = t \blacksquare_1 (c \blacksquare_2 p); t, c \in NTF \text{ and } p \in NTV;$$

$$(6) \text{ There exists any } t \in NTF \ni p \blacksquare_2 \text{neut}(t) = \text{neut}(t) \blacksquare_2 p = p; p \in NTV.$$

**Definition 2.4:** [26] Let  $(G, \nabla)$  be a NT group,  $(NTV, \nabla_1, \blacksquare_1)$  be a NT vector space on a NT field  $(NTF, \nabla_2, \blacksquare_2)$ , and  $g \nabla l \in NTV$  for  $g \in G, l \in NTV$ . If the following conditions are satisfied, then  $(NTV, \nabla_1, \blacksquare_1)$  is called NT G-module.

$$a) \text{ There exists } g \in G \ni k * \text{neut}(g) = \text{neut}(g) * k = k, \text{ for every } k \in NTV;$$

$$b) l \nabla_1 (g \nabla_1 h) = (l \nabla_1 g) \nabla_1 h, \forall l \in NTV; g, h \in G;$$

$$c) (r_1 \blacksquare_1 s_1 \nabla_1 r_2 \blacksquare_1 s_2) \nabla g = x \blacksquare_1 (h \nabla g) \nabla_1 y \blacksquare_1 (l \nabla g), \forall x, y \in NTF; h, l \in NTV; g \in G.$$

**Definition 2.5:** [23] The NT ring is a set endowed with two binary laws  $(M, *, \#)$  such that,

$$a) (M, *) \text{ is a abelian NT group; which means that:}$$

- $(M, *)$  is a commutative NT with respect to the law  $*$  (i.e. if  $x$  belongs to  $M$ , then  $neut(x)$  and  $anti(x)$ , defined with respect to the law  $*$ , also belong to  $M$ )
  - The law  $*$  is well – defined, associative, and commutative on  $M$  (as in the classical sense);
- b)  $(M, *)$  is a set such that the law  $\#$  on  $M$  is well-defined and associative (as in the classical sense);
- c) The law  $\#$  is distributive with respect to the law  $*$  (as in the classical sense)

**Definition 2.6:** Let  $(NTR, \nabla, \blacksquare)$  be a commutative NT ring and let  $(NTM, *, \circ)$  be a NT abelian group and  $\circ$  be a binary operation such that  $\circ: NTR \times NTM \rightarrow NTM$ . Then  $(NTM, *, \circ)$  is called a NT R-Module on  $(NTR, \nabla, \blacksquare)$  if the following conditions are satisfied. Where,

- 1)  $p \circ (r*s) = (p \circ r)* (p \circ s), \forall r, s \in NTM$  and  $p \in NTR$ .
- 2)  $(p \nabla k) \circ r = (p \nabla r) \circ (k \nabla r), \forall p, k \in NTR$  and  $\forall r \in NTM$
- 3)  $(p \blacksquare k) \circ r = p \blacksquare (k \circ r), \forall r, s \in NTR$  and  $\forall m \in NTM$
- 4) For all  $m \in NTM$ ; there exists at least a  $c \in NTR$  such that  $m \circ neut(c) = neut(c) \circ m = m$ . Where,  $neut(c)$  is neutral element of  $c$  for  $\blacksquare$ .

**Definition 2.7:** Let  $(NTM, *, \circ)$  be a NT R-Module on NT ring  $(NTR, \nabla, \blacksquare)$  and  $NTSM \subset NTM$ . Then  $(NTSM, *, \circ)$  is called NT R - submodule of  $(NTM, *, \circ)$ , if  $(NTSM, *, \circ)$  is a NT R – module on NT ring  $(NTR, \nabla, \blacksquare)$ .

**Definition 2.7:**  $(NTM_1, \circ_1)$  be a NT R-module on NT ring  $(NTR, \nabla, \blacksquare)$  and  $(NTM_2, *_2, \circ_2)$  be a NT R-module on NT ring  $(NTR, \nabla, \blacksquare)$ . A mapping  $f: NTM_1 \rightarrow NTM_2$  is said to be NT R-module homomorphism when

$$f((r \circ_1 m) *_1 (s \circ_1 n)) = (r \circ_2 f(m)) *_2 (s \circ_2 f(n)), \text{ for all } r, s \in \text{NTR and } m, n \in \text{NTM}_1.$$

**Definition 2.8:** Assume that  $(N_1, *)$  and  $(N_2, \circ)$  be two NETG's. If a mapping  $f: N_1 \rightarrow N_2$  of NETG is only one to one (injective)  $f$  is called neutro-monomorphism.

**Definition 2.9:** Let  $(N_1, *)$  and  $(N_2, \circ)$  be two NETG's. If a mapping  $f: N_1 \rightarrow N_2$  is only onto (surjective)  $f$  is called neutro-epimorphism.

**Definition 2.9:** Let  $(N_1, *)$  and  $(N_2, \circ)$  be two NETGs. If a mapping  $f: N_1 \rightarrow N_2$  neutro-homomorphism is one to one and onto  $f$  is called neutro-isomorphism. Here,  $N_1$  and  $N_2$  are called neutro-isomorphic and denoted as  $N_1 \cong N_2$ .

### 3. Quotient NTM and Neutro-Isomorphism

In this chapter, We prove neutro-isomorphism theorems. we define the quotient NTM and prove the fundamental theorem of neutro-homomorphism. We also prove the first neutro-isomorphism theorem for neutrosophic triplet Modules, the second neutro-isomorphism theorem for neutrosophic triplet Modules, the third neutro-Isomorphism theorem for neutrosophic triplet Modules and a few special cases.

**Definition 3.1:** Let  $\text{NTM}, \text{NTM}'$  be neutrosophic triplet left modules over the neutrosophic triplet ring  $R$ . A map  $\delta: \text{NTM} \rightarrow \text{NTM}'$  is called a neutrosophic triplet left  $R$ -module homomorphism if :

1.  $\delta$  is a neutrosophic triplet group neutro-homomorphism, that is if, for every  $m, n \in \text{NTM}$  we have  $\delta(m + n) = \delta(m) + \delta(n)$ ;
2. For every  $r \in R$  and for every  $m \in M$  we have  $\delta(r \cdot m) = r \cdot \delta(m)$

If  $\delta: \text{NTM} \rightarrow \text{NTM}'$  is a neutrosophic triplet  $R$ -module neutro-homomorphism we say that:

- i)  $\delta$  is a neutro-monomorphism if the map  $\delta$  is injective ;
- ii)  $\delta$  is a neutro-epimorphism if the map  $\delta$  is surjective ;
- iii)  $\delta$  is an isomorphism if the map  $\delta$  is bijective.

We will say that  $\text{NTM}$  and  $\text{NTM}'$  are neutro-isomorphic and we will write  $\text{NTM} \cong \text{NTM}'$  if there exists a neutro-isomorphism  $\delta: \text{NTM} \rightarrow \text{NTM}'$ . Observe that, in this case, the inverse map of  $\delta, \delta^{-1}: \text{NTM}' \rightarrow \text{NTM}$  is also a module isomorphism.

**Example 3.2.** Let  $R$  be a neutrosophic triplet ring. Given an element  $a \in R$  the map

$$\begin{aligned} \delta_a: R &\rightarrow R \\ r &\rightarrow r \cdot a \end{aligned}$$

is a left  $\text{NTM}$  neutro-homomorphism from  ${}_R R$  into  ${}_R R$ . Observe that, if  $a \neq \text{neut}(a)$ , then  $\delta_a$  is not a NTR neutro-homomorphism.

**Theorem 3.3.** Let  $R$  be a NTR, let  $M$  be a NTM and let  $H$  be a neutrosophic triplet  $R$ -Submodule. We define a left  $\text{NTM}$  structure on the neutrosophic triplet abelian group  $M/H$  by neutrosophic triplet setting, for every  $\dot{r} \in R$  and for every  $\dot{m} \in M, \dot{r} \cdot (\dot{m} + H) = (\dot{r} \cdot \dot{m}) + H$ . Moreover, with respect to this structure, the canonical projection  $\delta: M \rightarrow M/H$  becomes a surjective neutrosophic triplet  $R$ -module homomorphism.

**Proof.** We have first to show that (1) is well defined, that is, given any  $r \in R, m, m' \in M$  such that  $m+H = m'+H$  ( i.e.  $m-m' \in H$ ), we have that  $(r \cdot m)+H = r \cdot m'+H$  ( i.e.  $r \cdot m - r \cdot m' \in H$ ). But  $m - m' \in H$  implies that  $r \cdot m - r \cdot m' = r \cdot (m - m') \in H$  as  $H$  is a submodule of  $M$ . Let now  $k, l \in R, m, n \in M$ . We have:

$$k \cdot [(m + H) + (n + H)] = k \cdot [(m + n) + H] = (k \cdot (m + n)) + H = (k \cdot m + k \cdot n) + H = (k \cdot m + H) + (k \cdot n + H) = k \cdot (m + H) + k \cdot (n + H);$$

$$(k + l) \cdot (m + H) = ((k + l) \cdot m) + H = (k \cdot m + l \cdot m) + H = (k \cdot m + H) + (l \cdot m + H) = k \cdot (m + H) + l \cdot (m + H); (k \cdot l) \cdot (m + H) = ((k \cdot l) \cdot m) + H = (k \cdot (l \cdot m)) + H = k \cdot (l \cdot m + H) = k \cdot (l \cdot (m + H)); neut(k, l)_R \cdot (m + H) = (neut(k, l)_R \cdot m) + H = m + H.$$

Finally:  $\partial H (k \cdot m) = k \cdot m + H = k \cdot (m + H) = k \cdot \partial H (m)$ .

**Definition 3.4.** Let  $NTM$  be a neutrosophic triplet left module over a neutrosophic triplet ring  $R$  and let  $H$  be a neutrosophic triplet submodule of  $M$ . The neutrosophic triplet left  $R$ -module having the neutrosophic triplet quotient group  $M/H$  for its underlying neutrosophic triplet abelian group is called the neutrosophic triplet quotient module ( or a neutrosophic triplet factor module) of  $NTM$  modulo  $NTSM$  and is denoted by  $NTM/NTSM$ .

**Theorem 3.5.** Let  $R$  be a neutrosophic triplet ring and let  $\delta : NTM \rightarrow NTM'$  be a neutrosophic triplet left  $R$ -module neutro-homomorphism. If  $S$  is a  $NTSM$  of  $NTM$  contained in  $Ker(\delta)$ , then there exists a  $NTM$  neutro-homomorphism  $\bar{\delta} : NTM/NTSM \rightarrow NTM'$  such that the diagram commutes

i.e.  $\delta = \bar{\delta} \circ \partial S$ .

Moreover:

1.  $\bar{\delta}$  is unique with respect to this property;

2.  $Im(\delta) = Im(\bar{\delta})$  and  $Ker(\bar{\delta}) = Ker(\delta)/S$ ;

3.  $\bar{\delta}$  is injective  $\Leftrightarrow S = Ker(\delta)$ .

**Proof.** In view of the Fundamental Theorem for the a neutrosophic triplet quotient group there exists a a neutrosophic triplet group neutro-homomorphism  $\bar{\delta} : NTM/NTSM \rightarrow NTM'$  such that  $\delta = \bar{\delta} \circ \partial S$ .

Moreover: 1) such a neutrosophic triplet group neutro homomorphism is unique;

2)  $Im(\delta) = Im(\bar{\delta}), Ker(\bar{\delta}) = Ker(\delta)/S$ ;

3)  $\bar{\delta}$  is injective  $\Leftrightarrow S = Ker(\delta)$ .

Hence we only have to prove that, for every  $m \in NTM$  and  $r \in R$ :

$$\bar{\delta} (r(m + S)) = r \cdot \bar{\delta} (m + S).$$

It is now an easy calculation to arrive at:

$$\bar{\delta} (r \cdot (m+S)) = \bar{\delta} (r \cdot m+S) = \bar{\delta} (\partial S (r \cdot m)) = \delta (r \cdot m) = r \cdot \delta (x) = r \cdot \bar{\delta} (\partial S (m)) = r \cdot (m+S).$$

**Corollary 3.6. (First neutro-Isomorphism Theorem for NTM).**

Let  $R$  be a NTR and  $\delta : NTM \rightarrow NTM'$  be a NTLM neutro-homomorphism. Then the assignment

$$m + Ker(\delta) \rightarrow \delta (m)$$

defines an neutro-isomorphism of neutrosophic triplet left  $R$ -modules

$$\tilde{\delta} : NTM/Ker(\delta) \rightarrow Im(\delta)$$

In particular, if  $\delta$  is surjective, then  $\tilde{\delta}$  is an neutro isomorphism and

$$NTM/Ker(\delta) \cong NTM'.$$

**Theorem 3.7. (Second neutro-Isomorphism Theorem for NTM)**

Let  $H$  and  $B$  be NTSM of a NTM over a NTR. Then  $H \cap B$  and  $H + B$  are neutrosophic triplet submodules of NTM and the assignment  $m + (H \cap B) \rightarrow m + B$  defines an neutrosophic triplet  $R$ -module neutro-isomorphism from  $H / (H \cap B)$  into  $H + B / B$ . Therefore:

$$H / (H \cap B) \cong H + B / B$$

**Proof.** We know that  $H \cap B$  is a NTSM of NTM. Let  $r \in R, s \in H \cap B$ . Then  $rs \in H$  and  $rs \in B$ , as  $H$  and  $B$  are neutrosophic triplet submodules of NTM. Therefore  $r \cdot s \in H \cap B$ . We know that  $H + B$  is a neutrosophic triplet subgroup of NTM. Let  $r \in R, s \in H + B$ . Then there exist  $m \in H$  and  $n \in B$  such that  $s = m + n$ . Obviously  $rm \in H$  and  $rn \in B$ , and hence  $r \cdot s = r \cdot m + r \cdot n \in H + B$ . In view of the Second neutro-Isomorphism Theorem for neutrosophic triplet groups, the assignment  $m + (H \cap B) \rightarrow m + B$  defines a neutrosophic triplet group neutro-isomorphism  $\delta : H / (H \cap B) \rightarrow H + B / B$ . Let  $r \in R, m \in H$ , then we calculate:

$\delta (r(m + (H \cap B))) = \delta (rm + (H \cap B)) = rm + B = r(m + B) = r \delta (m + (H \cap B))$ . Therefore  $\delta$  is a neutrosophic triplet left  $R$ -module neutro-isomorphism.

**Theorem 3.8.** Let  $R$  be a NTR,  $\delta : NTM \rightarrow NTM'$  be a neutrosophic triplet left  $R$ -module neutro-homomorphism. For every neutrosophic triplet submodule  $S$  of  $M$  containing  $Ker(\delta)$  the assignment

$m + S \rightarrow \delta (m) + \delta (S)$  defines a neutro-isomorphism  $\hat{\delta} : M/S \rightarrow Im(\delta)/\delta(S)$ . Therefore

$$M/S \cong Im(\delta)/\delta(S).$$

**Proof.** We know that the assignment  $m + S \rightarrow \delta (m) + \delta(S)$  defines a neutrosophic triplet group neutro-isomorphism  $\pi = \hat{\delta}_N : M/S \rightarrow Im(\delta)/S$ .

Let  $r \in R, m \in S$ . We have :



$\pi(r(m+S)) = \pi(rm+S) = \delta(rm) + \delta(S) = (r\delta(m)) + \delta(S) = r(\delta(m) + \delta(S)) = r\pi(m+S)$  Therefore  $\pi$  is a neutrosophic triplet left  $R$ -module neutro-isomorphism.

### Corollary 3.9. (Third neutro-Isomorphism Theorem for NTM)

Let  $H$  and  $B$  be neutrosophic triplet submodules of a NTM over a NTR and assume that  $H \subseteq B$ .

Then the assignment  $m+B \rightarrow (m+H)+H/B$ . Defines a neutrosophic triplet left  $R$ -module neutro-isomorphism from  $M/B$  into  $(M/H)+H/B$ . Therefore

$$M/B \cong (M/H)+H/B$$

Proof. Apply Theorem 3.8 to  $\partial_H : M \rightarrow (M/H)+H$ , recalling that  $\partial_H(B) = (B+H)/H$ .

## 4. Conclusions

This article mainly focused on fundamental homomorphism theorems for neutrosophic  $R$ -modules. We gave and proved the fundamental theorem of neutro-homomorphism, as well as first, second and third neutro-isomorphism theorems explained for NTM. Furthermore, we define neutro-monomorphism, neutro-epimorphism. By applying them to neutrosophic algebraic structures. We looked at it as closely related as different systems. Using the concept of the fundamental theorem of neutro-Homomorphism and neutro-isomorphism theorems, the relationship between neutrosophic algebraic structures was studied.

## Abbreviations

NT: Neutrosophic triplet

NTS: Neutrosophic triplet set

NETG: Neutrosophic extended triplet group

NTM: Neutrosophic triplet  $R$ -module

NTSM: Neutrosophic triplet  $R$ -submodule

NTLM: Neutrosophic triplet left  $R$ -module

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